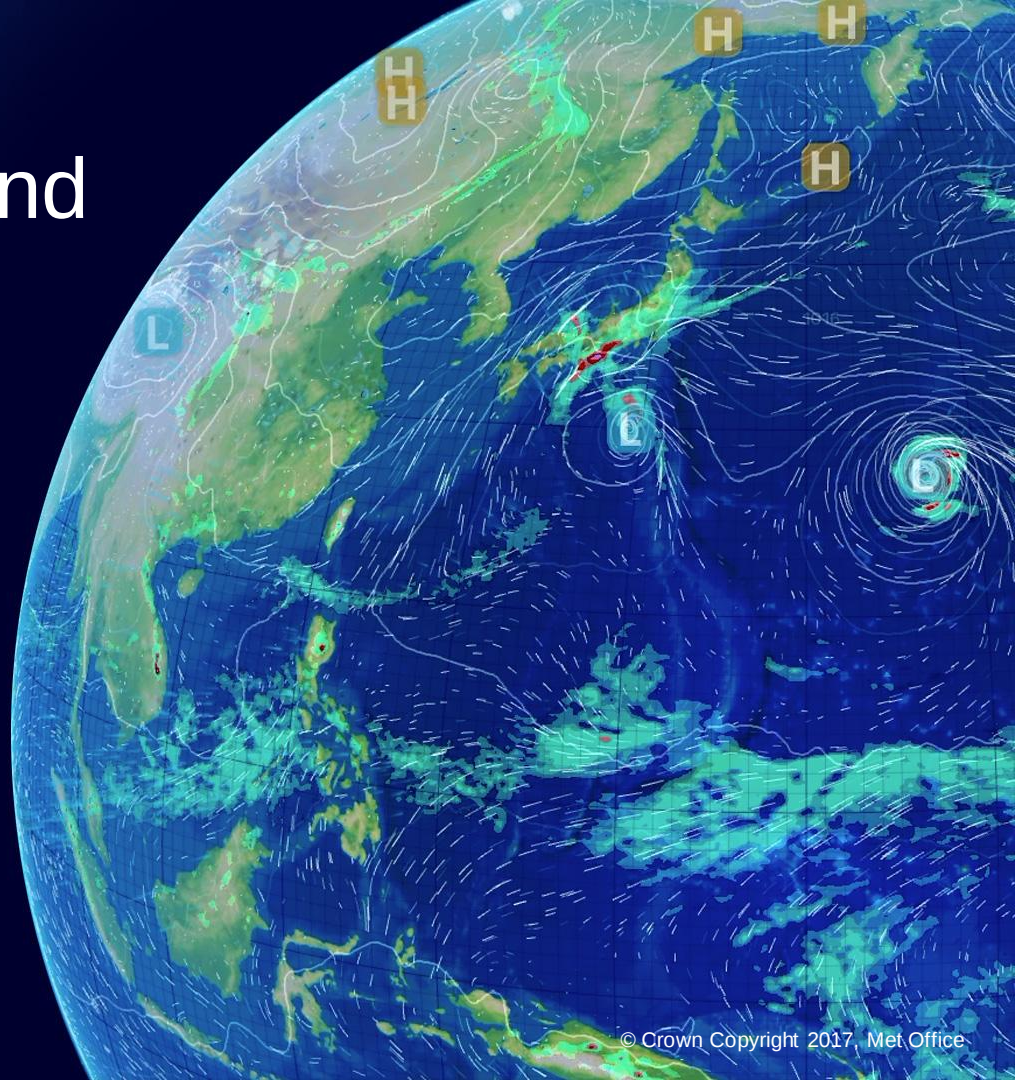


Predictability barriers and diabatic processes

Claudio Sanchez, John Methven, Mike Cullen

NAWDEX workshop

Toulouse, 26/03/2019

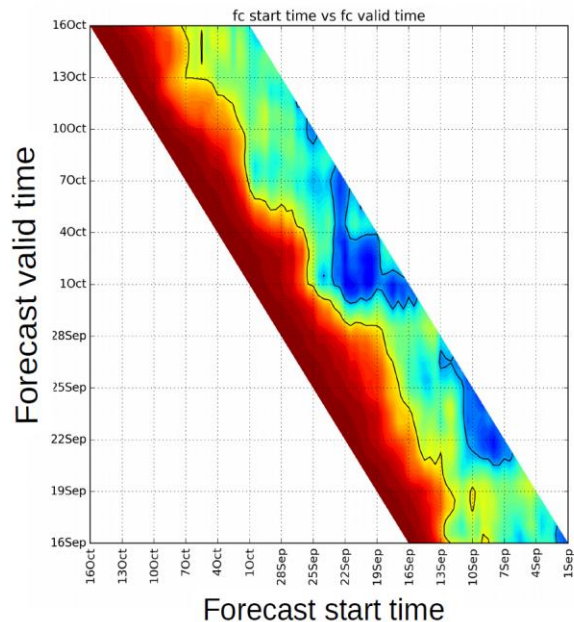


Outline

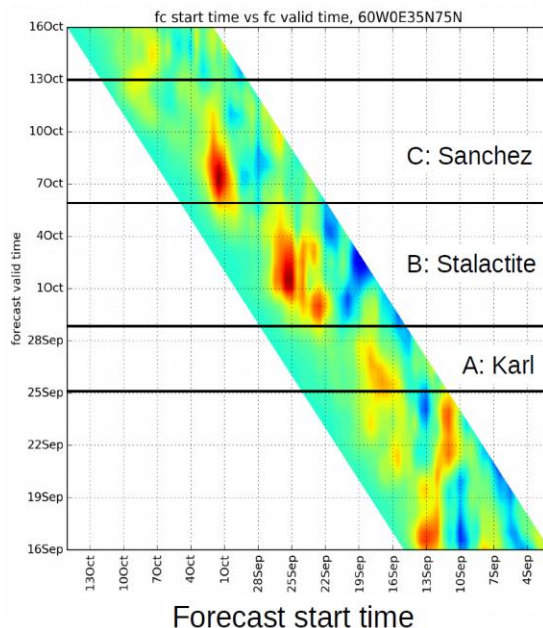
- Revisiting predictability barriers from George's talk last year
- Predictability barriers for UM and EC det. and UM Ensemble during NAWDEX period (15 Sept. to 15 Oct 2016)
- Semi-Geostrophic (SG) inversion model: tracking footprints of diabatic processes
- Results from SG model and diabatic tracers from a pseudo-operational MetUM

Predictability barriers

ACC as function of
start and valid time



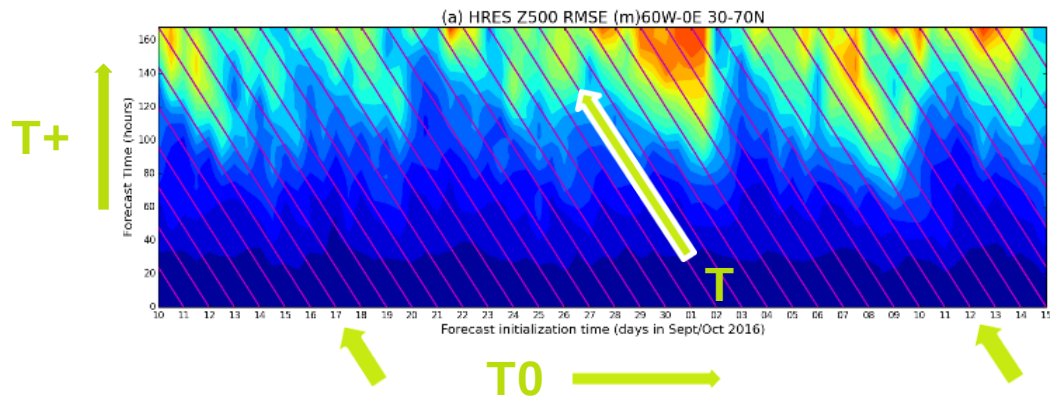
Rate of change of ACC



Rate of change of
ACC for *ECMWF*
Z500 increases at
particular validation
times, defined as
“predictability
barriers”

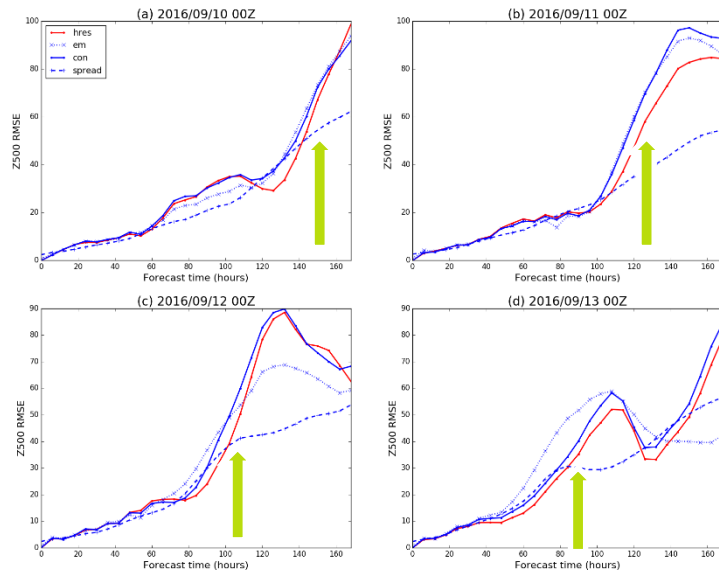
Craig et al. (2018): Predictability barriers, NAWDEX 2018 workshop, Munich

Predictability barriers (2)



Error T+ profiles for forecasts initialized at 00Z (a) 10 , (b) 11, (c) 12 and (d) 13 9/2016.

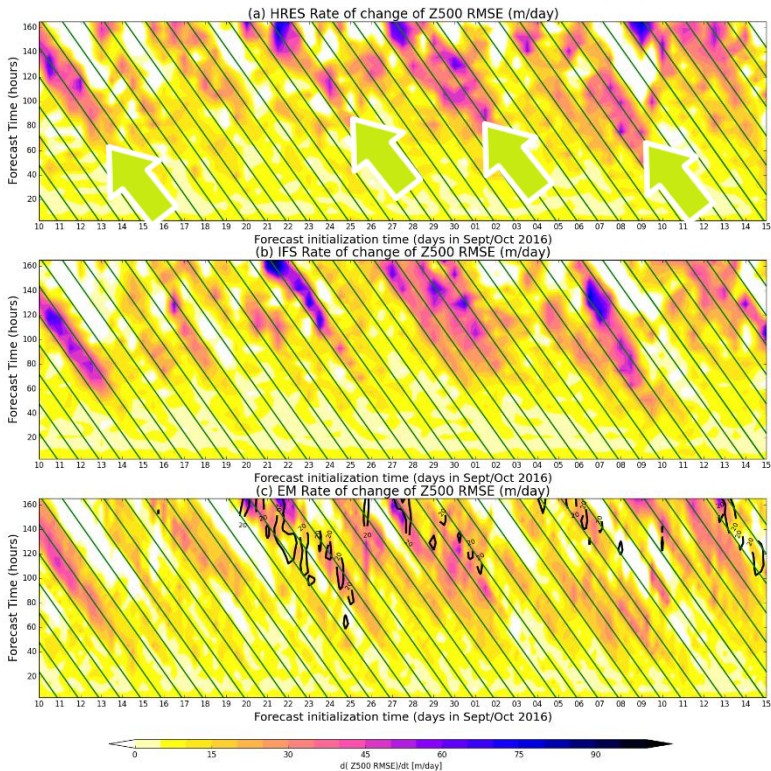
Skill drops suddenly around 16th 12Z (T+156, T+132, T+108, T+84)



Error in 2D: Init. time 'T0' vs validation time 'T+'
Events that generate **larger errors are clear** and attributable to particular periods.

Some of the **events occur in the same day** regardless of the forecasts time (e.g. 17/09 or 12/10)
[Follow 'validation time' diagonal lines]

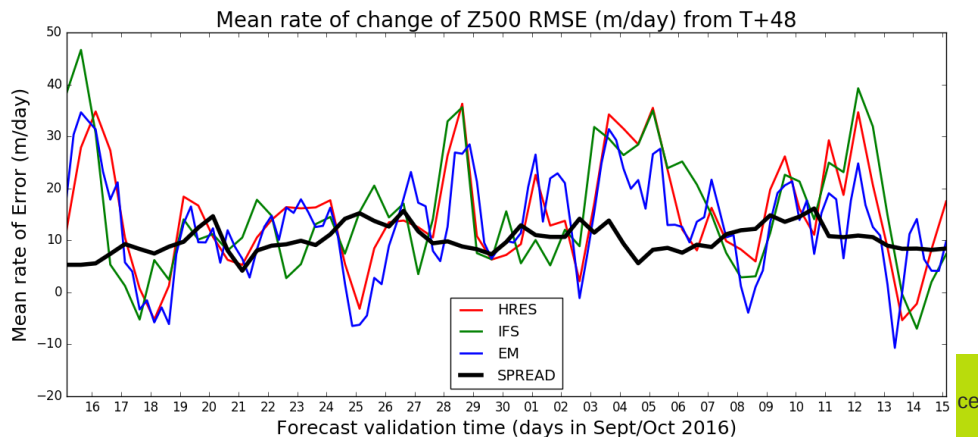
Predictability barriers (3)



Doing the error tendency ($\partial \text{'error'} / \partial \text{'T+'}$):
Clear signal of forecast skill drop for given days (16th + 29th Sept, 5th + 12th Oct).

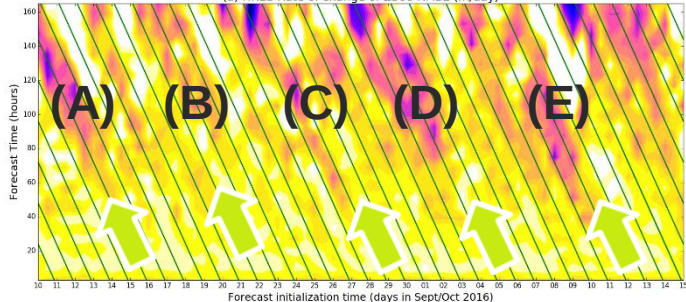
Predictability barriers!!

Σ validation time: Spread insensitive to barriers!



NAWDEX and SG results

(a) HRES Rate of change of Z500 RMSE (m/day)



(A): 16th-18th Sept. *Ex-TC Ian*. IOP 1

(B): 22nd-23th Sept. *Vladiana* IOP 4

(C): 28-29th Sept. *Walpurga* + *Ex-TC Karl*. IOP 5

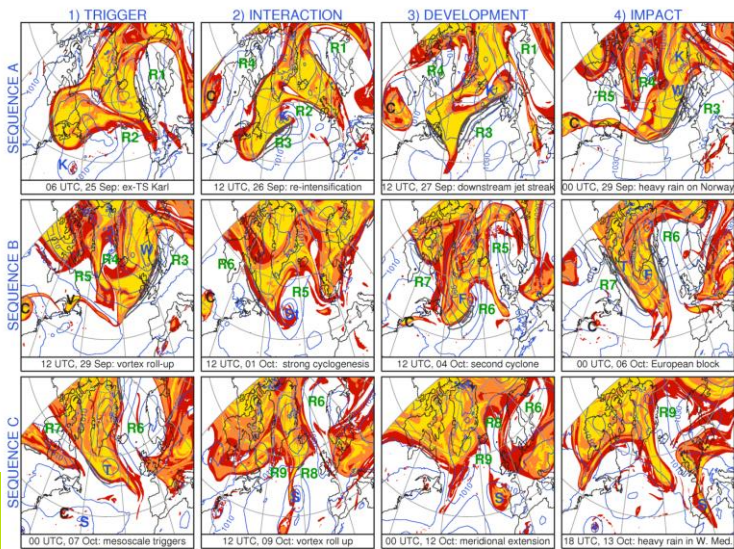
SEQUENCE A

(D): 4th-6th Oct. Downstream effects of *Stalactite* cyclone + blocking development. IOP 6-7

SEQUENCE B

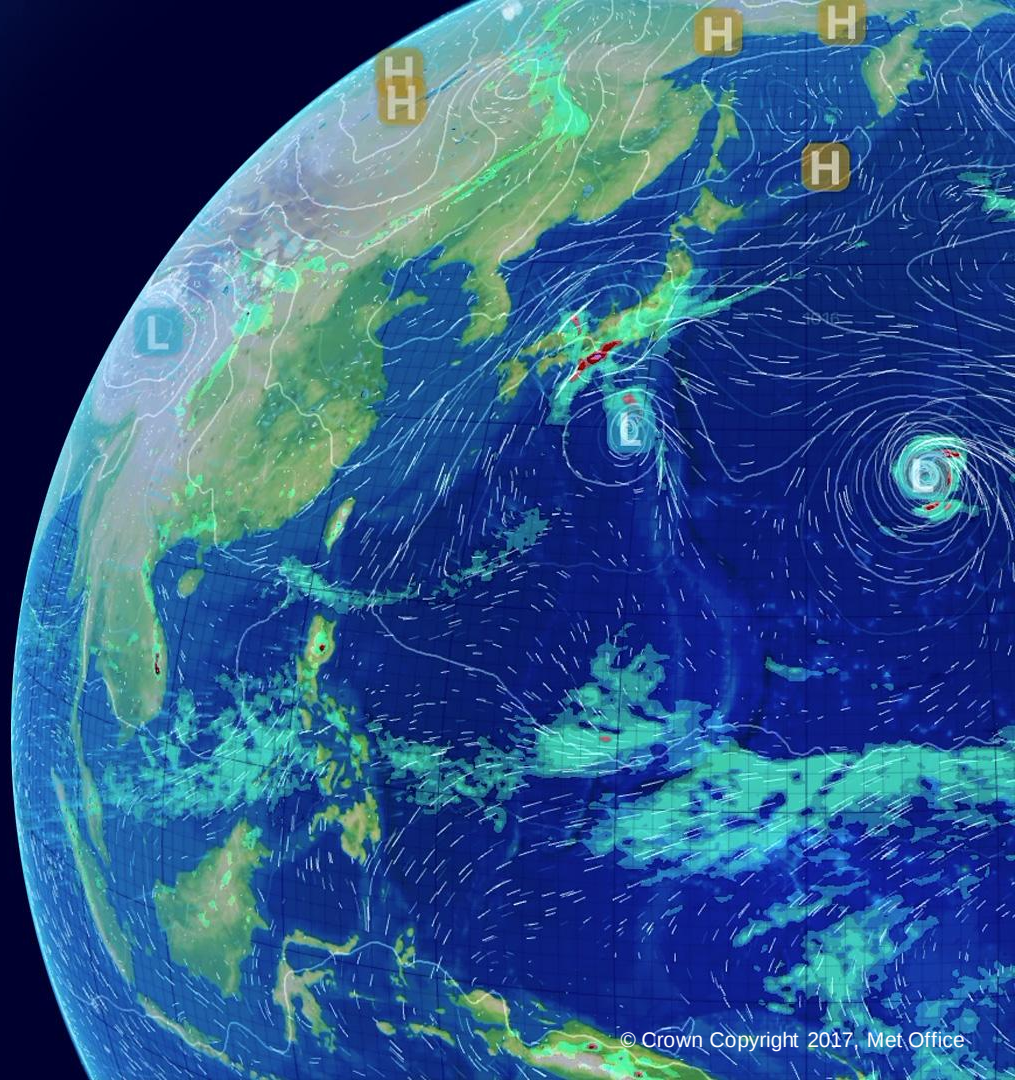
(E): 11-13th Oct. PV cut off *Sanchez* + tropopause ridge *Thor*. IOP 9-10

SEQUENCE C



[Left] NAWDEX golden cases (aka Sequences)
Fig 6. Schaffler et al. 2018

Linking predictability barriers to diabatic processes ...



Met Office Semi-Geostrophic (SG) Inversion Model

UM eqs:

$$\frac{D\mathbf{u}}{Dt} + c_{pd}\theta_v\nabla\pi + 2\Omega \times \mathbf{u} = \mathbf{g} + \frac{\partial}{\partial r} \left(K_m \frac{\partial \mathbf{u}_h}{\partial r} \right) + S_{\mathbf{u}},$$

$$\frac{D\theta_{vd}}{Dt} = S_{\theta_{vd}},$$

+

Π : Exner pressure

K_m : BL diffusion coef.

S : Source terms

$\mathbf{v}_e$: Geostrophic wind

SG eq:

$$c_{pd}\theta_v\nabla_h\pi - (fv_e, -fu_e) = \frac{\partial}{\partial r} \left(K_m \frac{\partial \mathbf{u}_e}{\partial r} \right)$$

$$c_{pd}\theta_v \frac{\partial \pi}{\partial r} = -g.$$



$$\mathbf{BQ}' \begin{pmatrix} u - u_e \\ v - v_e \\ w \end{pmatrix} + c_{pd}\theta_v \frac{\partial}{\partial t} \begin{pmatrix} \frac{1}{r \cos \phi} \left(\frac{\partial \pi}{\partial \lambda} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \lambda} \right) \\ \frac{1}{r} \left(\frac{\partial \pi}{\partial \phi} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \phi} \right) \\ \frac{\partial \pi}{\partial r} \end{pmatrix} = \mathbf{BH}'$$

$$\mathbf{H}' = \begin{pmatrix} -(\mathbf{u}_e\theta_v) \cdot \nabla \left(\frac{v_e}{\theta_v} \right) + S_v - \frac{v_e S_{\theta_v}}{\theta_v} \\ (\mathbf{u}_e\theta_v) \cdot \nabla \left(\frac{u_e}{\theta_v} \right) - S_u + \frac{u_e S_{\theta_v}}{\theta_v} \\ -\mathbf{u}_e \cdot \nabla \theta_v + S_{\theta_v} \end{pmatrix}$$

SG model able to solve pressure tendency ($d\pi/dt$), ageostrophic wind ($\mathbf{v} - \mathbf{v}_e$) and balanced vertical wind (w).

Source Matrix H' : linear comb. of geostrophic term plus friction and diabatic sources

More info in **Cullen (2018)**: *The Use of Semigeostrophic Theory to Diagnose the Behaviour of an Atmospheric GCM*, fluids 3,72



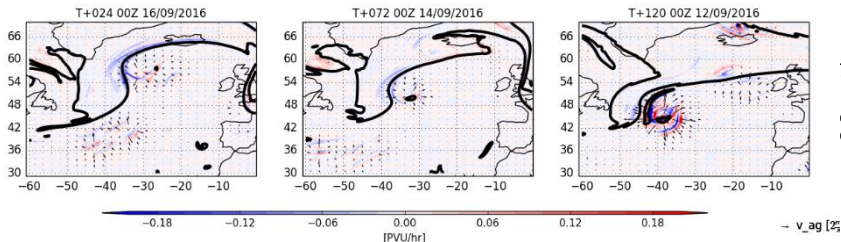
Met Office SG and predictability barriers

SG model integrated for one hour from pseudo-operational Met-UM (17km) at T+1,3,5 D. Only diabatic sources (S_θ) are considered.

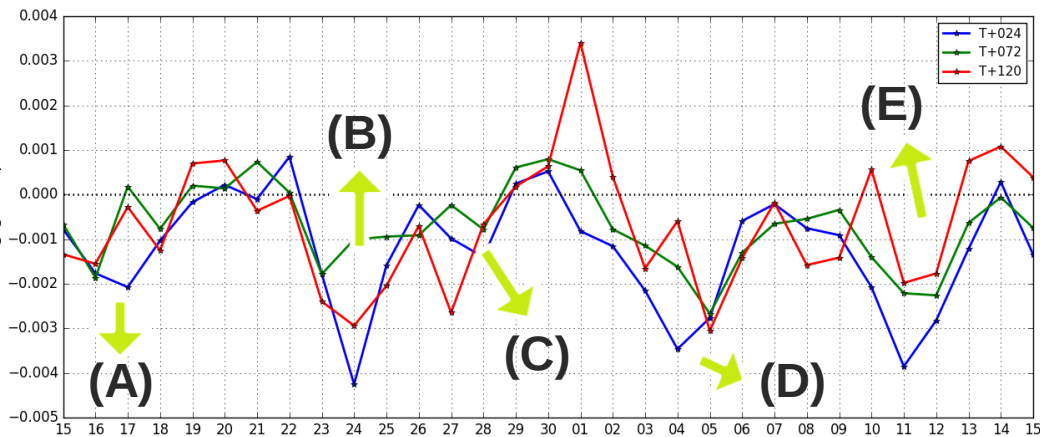
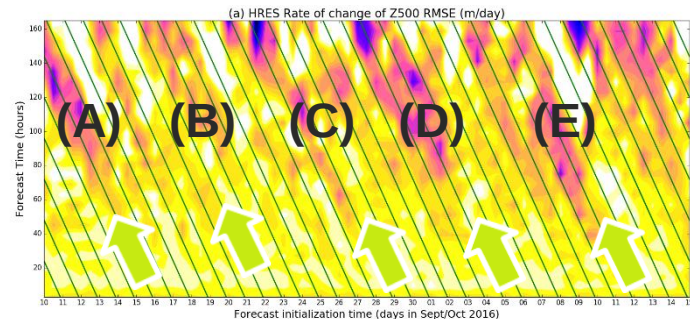
$$-v_{ag}(diab) \cdot \nabla q$$

Ageostrophic advection of PV shows areas where there are cross-tropopause and ridge building action

00Z 17/09/2016 L37 (9621m)



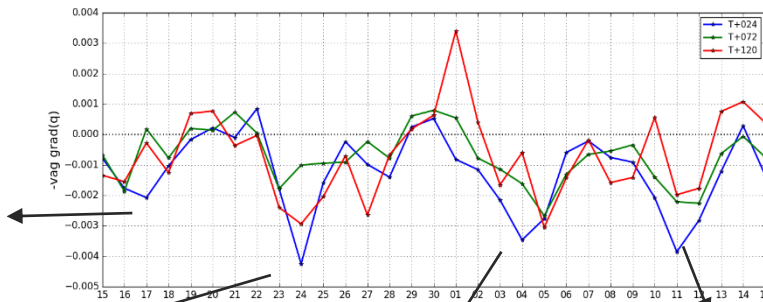
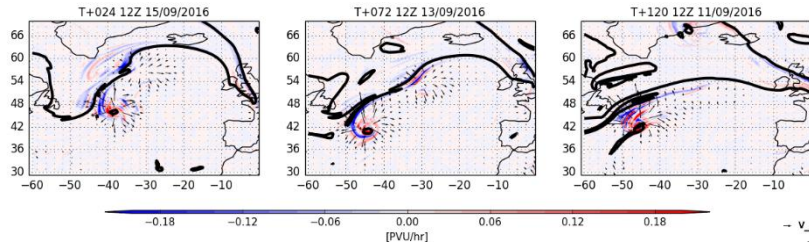
[Top]: $v_{ag}(diab) \cdot \nabla q$ for 17th 00Z Sept. Ridge building delayed in longer forecasts



[Top]: $v_{ag}(diab) \cdot \nabla q$ averaged over the predictability barrier domain (60-0E, 30-70N). Dims: PVU/hr

(lan: 16 12Z)

12Z 16/09/2016 L37 (9621m)

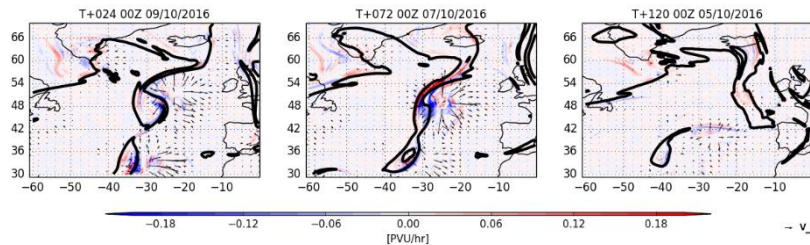
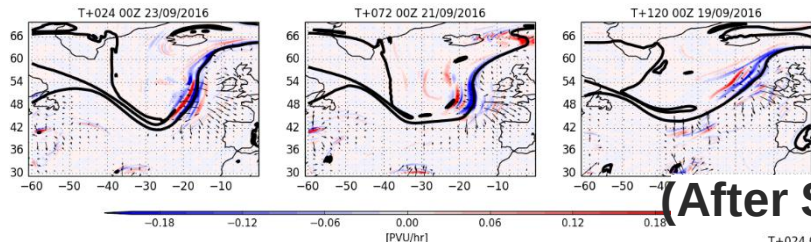


(Sanchez. 10 00Z)

00Z 10/10/2016 L37 (9621m)

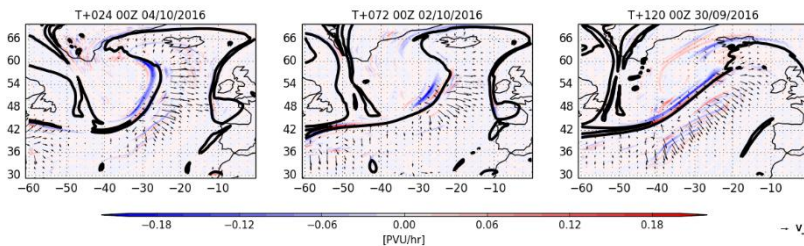
(Vladiana: 24 00Z)

00Z 24/09/2016 L37 (9621m)



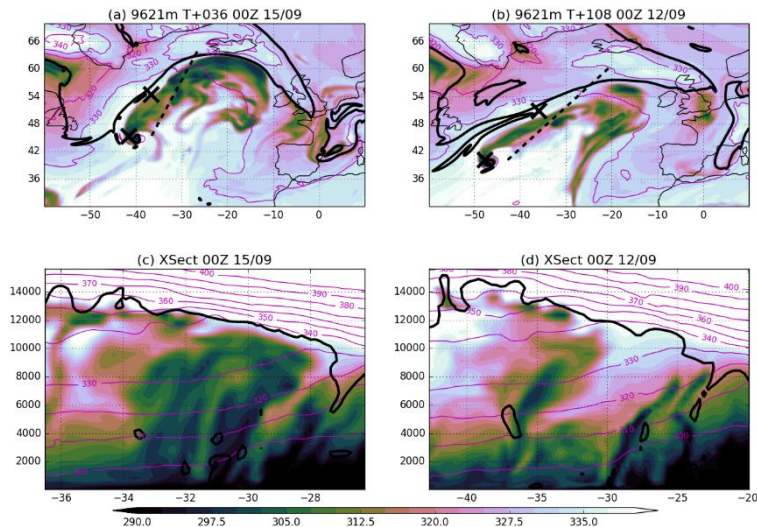
(After St. 5 00Z)

00Z 02/10/2016 L37 (9621m)



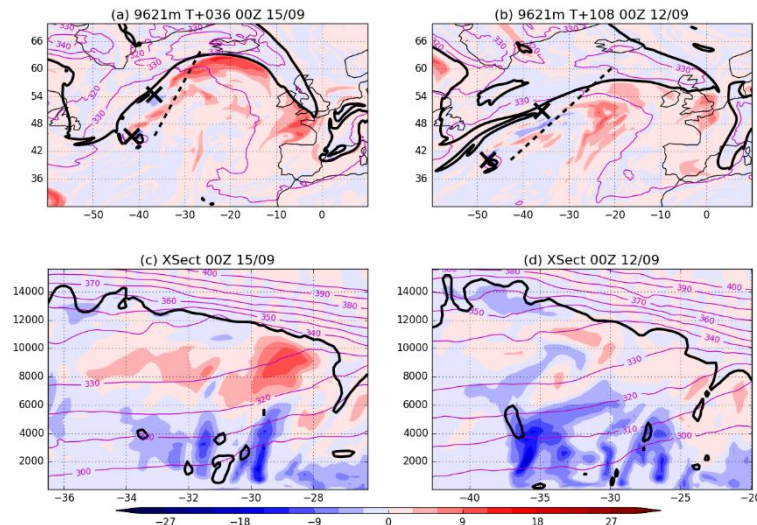
Ex-TC IAN (IOP1)

dtheta_0 12Z 16/09/2016



Longer forecast fail to merge, important ascent and heating from LS-rain over ridge

dtheta_mic 12Z 16/09/2016

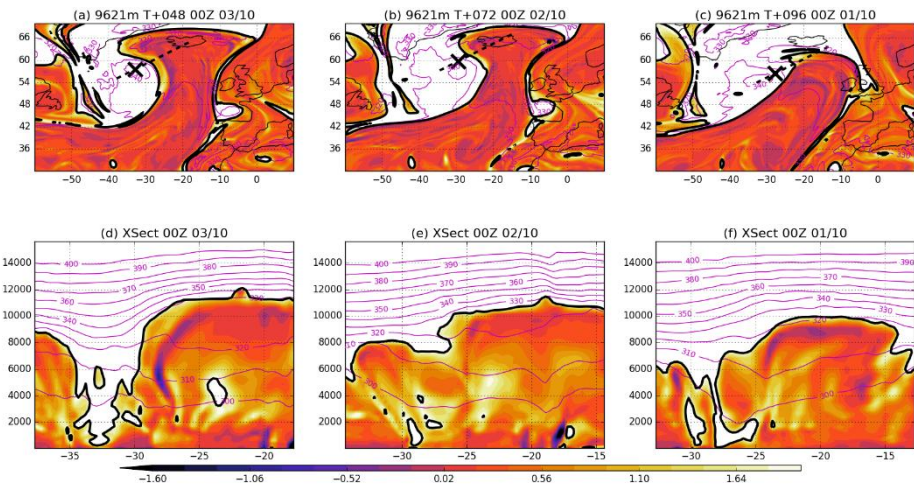


[Top] 'advection only $d\theta$ ' tracer on 12Z 16th for (a,c) 00Z 15th (b,d) 00Z 12th forecast. (c,d) Cross section on dashed line in (a,b). X: Pos of Ian and merged cyclone. Tracer initialized at 00Z 15th

[Top] Same as left, but for $d\theta_{LS}$.

After stalactite (IOP6?)

pv 00Z 05/10/2016

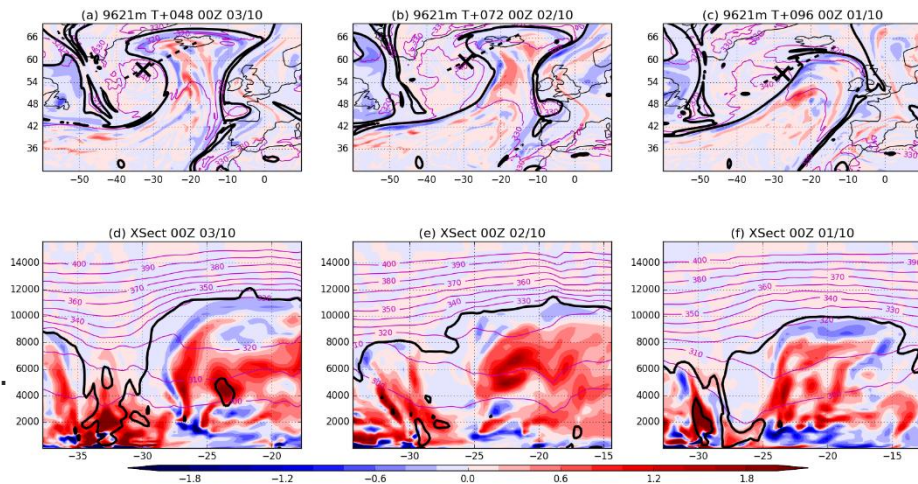


[Top]: PV on 00Z 5th in different forecasts initialized at 00Z 3rd, 2nd and 1st. X shows the position of the stalactite's upstream cyclone.

[Right]: same layout for dPV_{LS} tracer (initialized at 00Z 3rd).

Delay in ridge building, strong negative PV filament associated to LS rain process

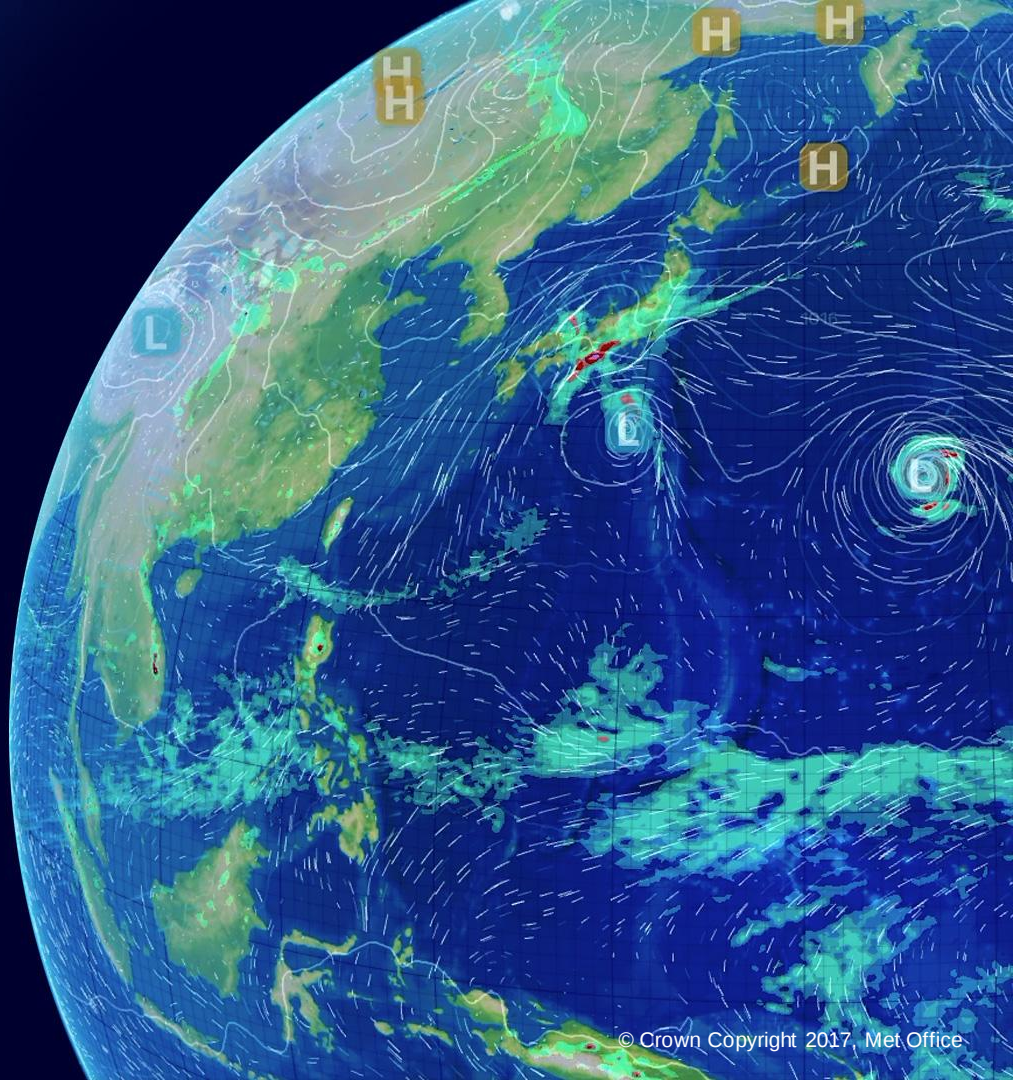
dPV_{mic} 00Z 05/10/2016



Conclusions

- Predictability barriers coincide with important IOP NAWDEX cases (Ian, Karl, Stalactite, Sanchez). Both EC and UM struggle
- UM EPS fail to capture rapid increase of model error
- Semi Geostrophic inversion model provides a neat way to convey the influence of diabatic processes in the flow (“diabatic ageostrophic advection” of PV $-v_{ag}(diab) \cdot \nabla q$)
- Peaks of diabatic ageostrophic advection coincide with predictability barriers, less advection is produced in longer forecasts

*Thanks for your
attention!*





$$\mathbf{BQ}' \begin{pmatrix} u - u_e \\ v - v_e \\ w \end{pmatrix} + c_{pd} \theta_v \frac{\partial}{\partial t} \begin{pmatrix} \frac{1}{r \cos \phi} \left(\frac{\partial \pi}{\partial \lambda} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \lambda} \right) \\ \frac{1}{r} \left(\frac{\partial \pi}{\partial \phi} - \frac{\partial \pi}{\partial r} \frac{\partial r}{\partial \phi} \right) \\ \frac{\partial \pi}{\partial r} \end{pmatrix} = \mathbf{BH}' \quad \text{Where}$$

$$\mathbf{B} = \begin{pmatrix} f & -\frac{\partial}{\partial r} \left(K_m \frac{\partial}{\partial r} \right) & 0 \\ \frac{\partial}{\partial r} \left(K_m \frac{\partial}{\partial r} \right) & f & 0 \\ 0 & 0 & g/\theta_v \end{pmatrix}$$

$$\mathbf{Q}' = \begin{pmatrix} f + \frac{\theta_v}{r \cos \phi} \frac{\partial}{\partial \lambda} \left(\frac{v_e}{\theta_v} \right) + \frac{u_e \tan \phi}{r} & \frac{\theta_v}{r} \frac{\partial}{\partial \phi} \left(\frac{v_e}{\theta_v} \right) + \frac{\partial}{\partial r} \left(K_m \frac{\partial}{\partial r} \right) & \frac{\theta_v}{r} \frac{\partial}{\partial r} \left(\frac{v_e}{\theta_v} \right) \\ -\frac{\theta_v}{r \cos \phi} \frac{\partial}{\partial \lambda} \left(\frac{u_e}{\theta_v} \right) + \frac{v_e \tan \phi}{r} - \frac{\partial}{\partial r} \left(K_m \frac{\partial}{\partial r} \right) & f - \frac{\theta_v}{r} \frac{\partial}{\partial \phi} \left(\frac{u_e}{\theta_v} \right) & -\frac{\theta_v}{r} \frac{\partial}{\partial r} \left(\frac{u_e}{\theta_v} \right) \\ \frac{1}{r \cos \phi} \frac{\partial \theta_v}{\partial \lambda} & \frac{1}{r} \frac{\partial \theta_v}{\partial \phi} & \frac{\partial \theta_v}{\partial r} \end{pmatrix}$$

Elliptic equation for $\partial \pi / \partial t \rightarrow$

$$\frac{\kappa_d - 1}{\kappa_d} \frac{\rho_d}{\pi} r^2 \frac{\partial r}{\partial \eta} \frac{\partial \pi}{\partial t} + r^2 \frac{\partial r}{\partial \eta} \frac{\rho_d c_{pd} \theta_v^2}{g \theta_{vd}} \frac{\partial}{\partial t} \left(\frac{1}{(1+\mu)} \frac{\partial \pi}{\partial r} \right) + \nabla \cdot \left(r^2 \rho_d c_{pd} \theta_v \frac{\partial r}{\partial \eta} \mathbf{R} \mathbf{P}^{-1} \frac{\partial}{\partial t} (\nabla_r \pi) \right) = \nabla \cdot \left(r^2 \rho_d \frac{\partial r}{\partial \eta} \mathbf{R} \mathbf{P}^{-1} \mathbf{G} \right) + \frac{1}{\cos \phi} \left(\frac{\partial}{\partial \lambda} \left(r \rho_d u_e \frac{\partial r}{\partial \eta} \right) + \frac{\partial}{\partial \phi} \left(r \rho_d v_e \cos \phi \frac{\partial r}{\partial \eta} \right) \right).$$

Vertical velocity can be deduced using the S-G omega equation.

Its form in momentum coordinates (Hoskins & Draghici, 1977) is:

$$\nabla_X^2 \left(\frac{g \rho_r}{\theta_0 f_0} q_g w^* \right) + f_0^2 \frac{\partial^2 w^*}{\partial Z^2} = \boxed{2 \nabla_X \cdot \mathbf{Q}} + \boxed{\nabla_X^2 H} \quad H = \alpha w^*, \quad \hat{Z} = \frac{N_0}{f_0} Z$$

Geostrophic
forcing

Diabatic forcing
(H=heating)

