

NAWDEX Workshop
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Modification of potential temperature and PV in forecasts of different lead times

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- Lagrangian tracers and on-line trajectories enable an unprecedented level of detail in model output
 - These techniques allow us to follow air parcels (in model world) while still solving an Eulerian model
- We can use them to study processes behind phenomena
 - Air-mass modification around cyclones (e.g. Oertel et al. 2018)
 - Predictability barriers (Claudio's talk)
- We can also use them to study model error (Saffin et al. 2017)
- Can we use them to identify systematic model error structure in model tendencies?

Approach

- Describe modification at a given grid-point

- In purely Eulerian terms

$$\theta(x, t) = \theta(x, t = 0) + \Delta\theta(x, t)$$

- In terms of Lagrangian tracers

$$\theta(x, t) = \theta_0(x, t) + \delta\theta(x, t)$$

- Assume a theoretical unbiased model (no systematic error)

$$\langle \epsilon \rangle = 0$$

- Compare 12-h v 24-h forecasts from operational model against the expected behaviour of the theoretical unbiased model

Data

- Variables of interest: Potential temperature and PV
- NAWDEX field campaign: 17 September – 22 October 2016 (Schäfler et al. 2017)
- Met Office MetUM vn10.4 hindcasts, including diabatic tracers
 - Here including only forecasts between 0000 UTC 20 September – 1200 UTC 14 October 2016 every **12 hours**
- Global N768 (17 km at 50° latitude)
- Output on 20°N – 80°N, 80°W – 40°E
 - 197890 grid points per level
 - **Statistically robust analysis** over 10 model levels, i.e. $\sim 2 \times 10^6$ grid points per day and $\sim 10^8$ grid points in the dataset

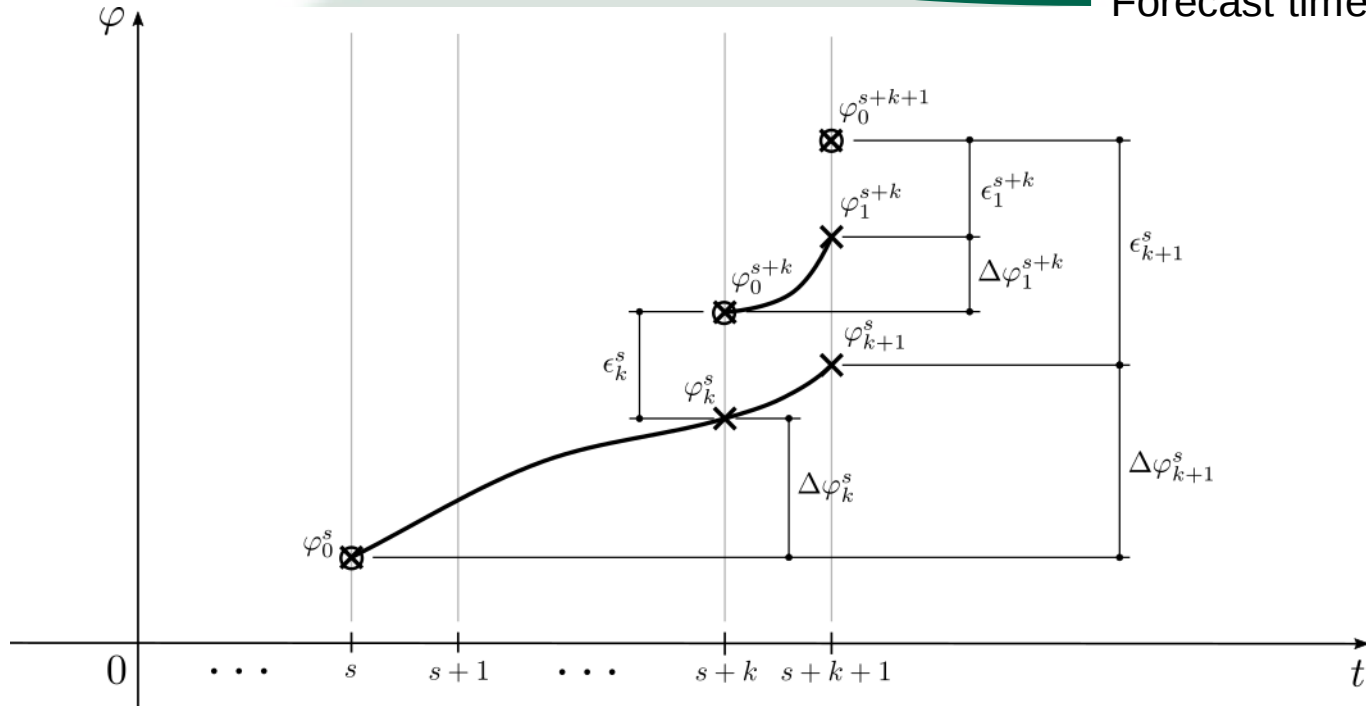
Eulerian description

On a given grid point:

$$\varphi_n^m = \varphi_n^m(\mathbf{x})$$

Forecast base time

Forecast time step



$$(\Delta\varphi_{k+1}^s - \Delta\varphi_k^s) - \Delta\varphi_1^{s+k} = \epsilon_1^{s+k} - \epsilon_{k+1}^s + \epsilon_k^s$$

For an unbiased model:

$$\langle \Delta\varphi_{k+1}^s - \Delta\varphi_k^s \rangle - \langle \Delta\varphi_1^{s+k} \rangle = 0$$

Lagrangian-tracer description

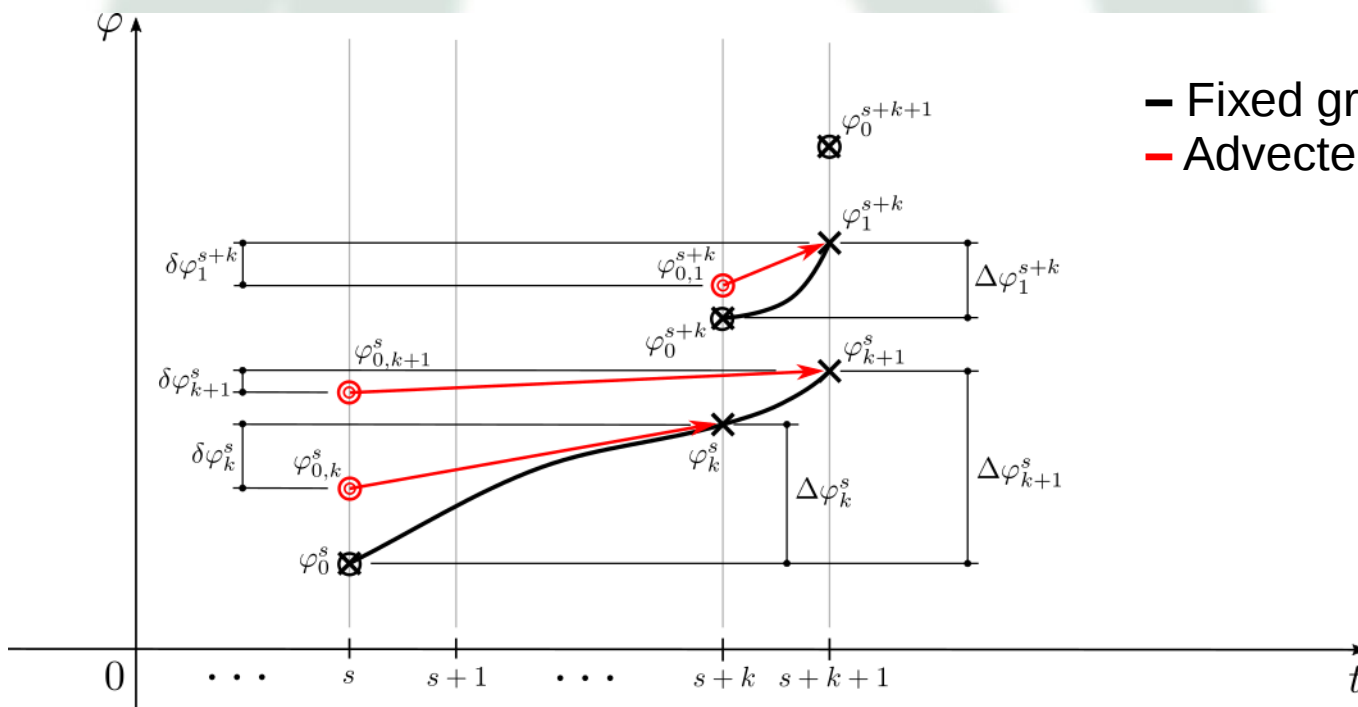
Still on a given grid point:

Parcel's initial φ -value (at forecast base time m)
advected to the grid point
at forecast time step n

$$\varphi_n^m = \varphi_{0,n}^m + \delta\varphi_n^m$$

φ -increment due to
parametrised diabatic
processes

$$\Delta\varphi_n^m = \delta\varphi_n^m + (\varphi_{0,n}^m - \varphi_0^m)$$



Lagrangian-tracer description

For an unbiased model:

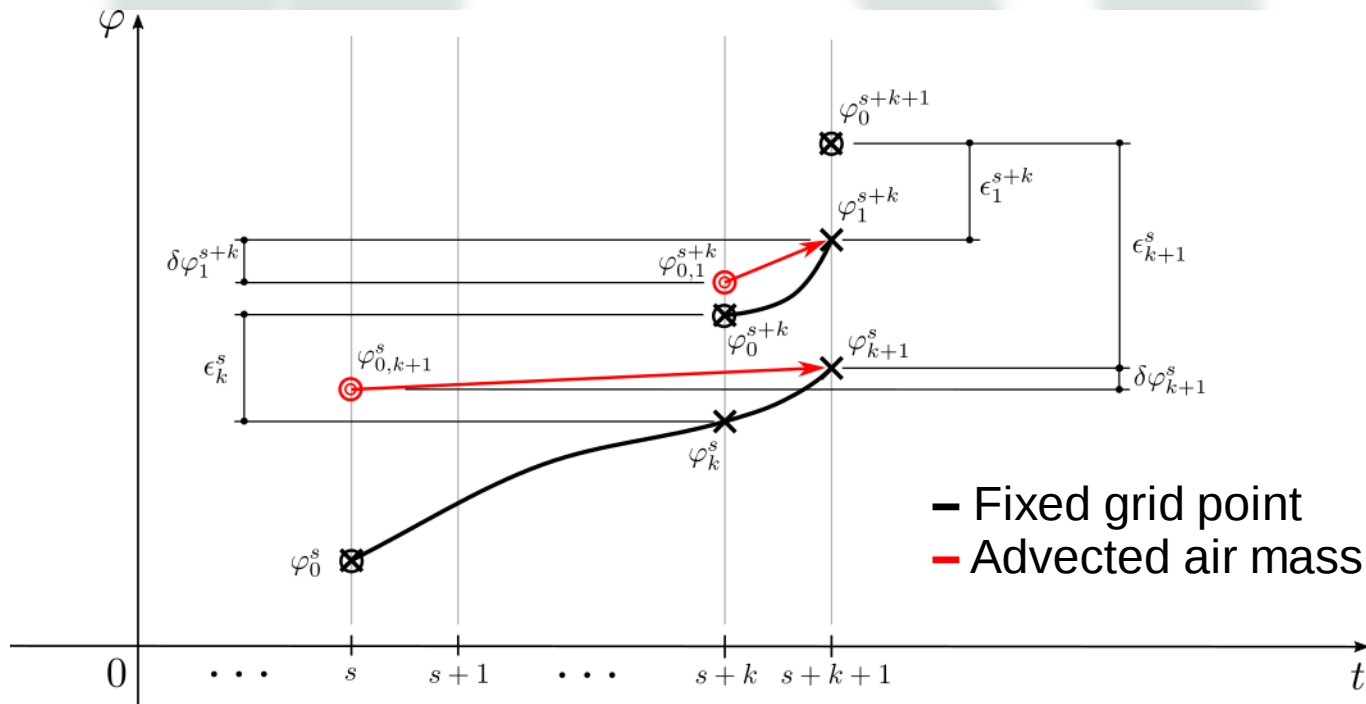
$$\langle \varphi_{0,k \rightarrow k+1}^s - \varphi_{0,0 \rightarrow 1}^{s+k} \rangle + \langle \delta \varphi_{k+1}^s - \delta \varphi_1^{s+k} \rangle = 0$$

where

Advection

Along-trajectory
modification

$$\varphi_{0,n \rightarrow m}^s = \varphi_{0,m}^s - \varphi_n^s$$



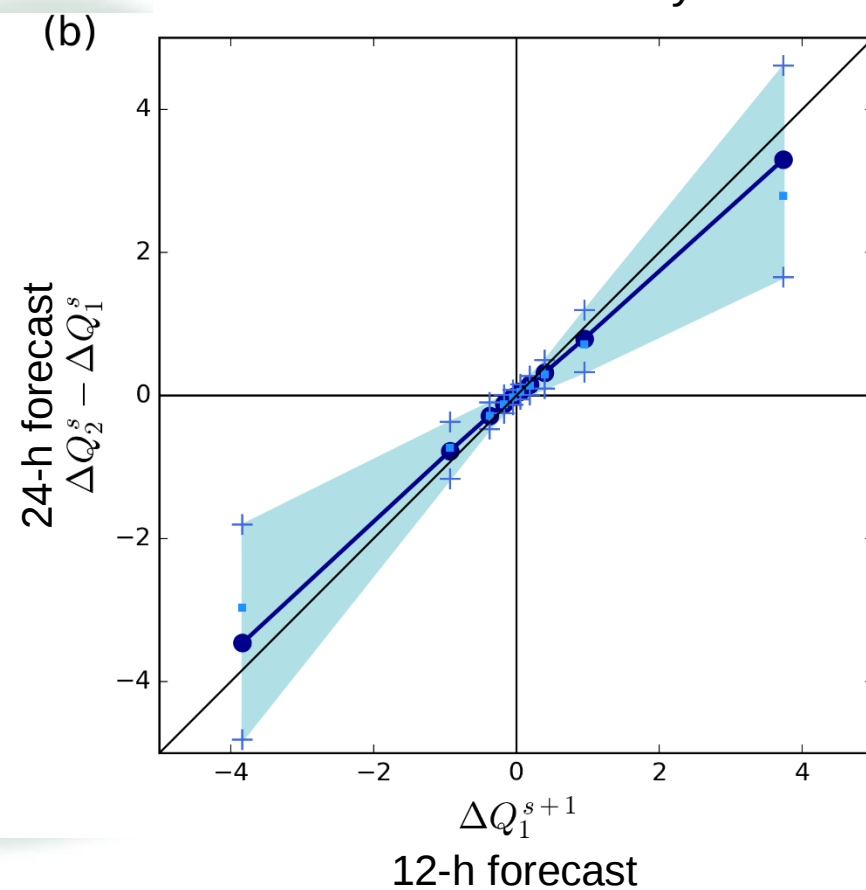
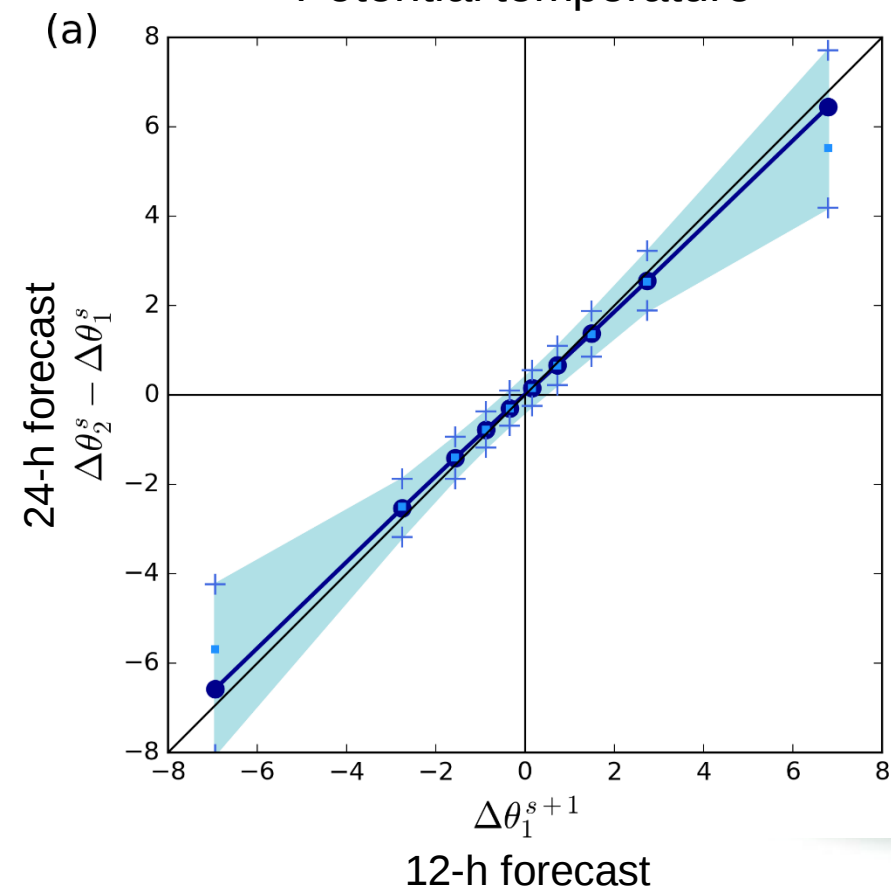
Eulerian description

$$\langle \Delta\varphi_{k+1}^s - \Delta\varphi_k^s \rangle = \langle \Delta\varphi_1^{s+k} \rangle$$

Upper levels (6.8 km – 11.2 km)

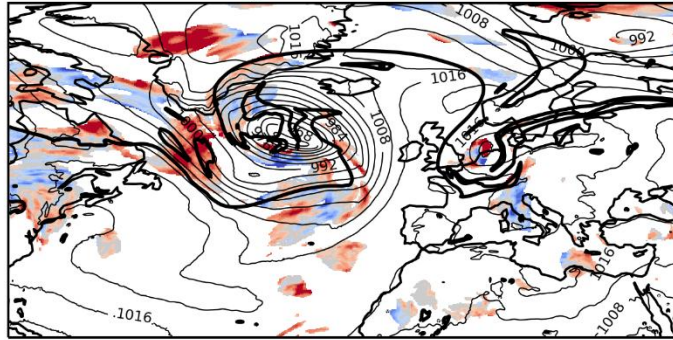
Potential temperature

Potential vorticity

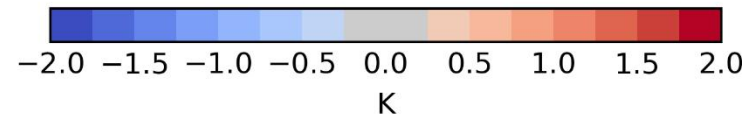
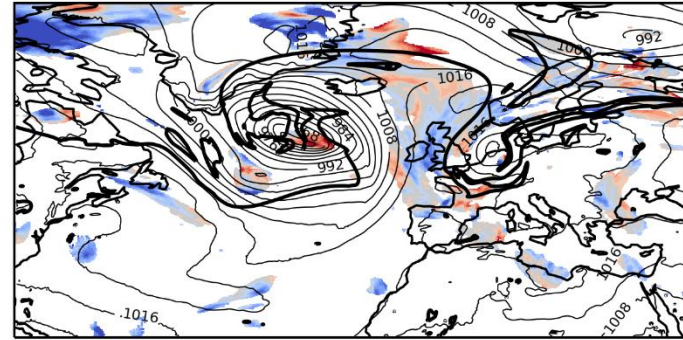


Eulerian description

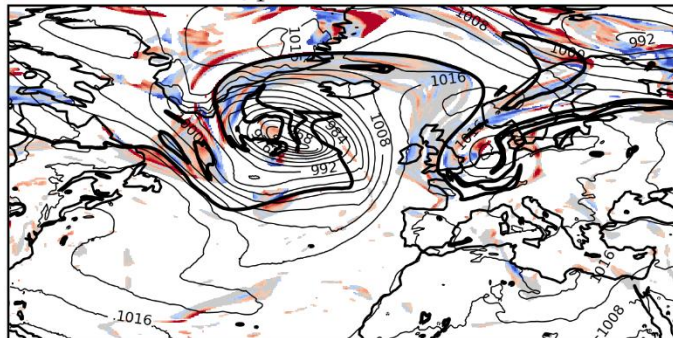
(a) $\Delta\theta_1^{s+1} < 2^{\text{nd}}$ decile



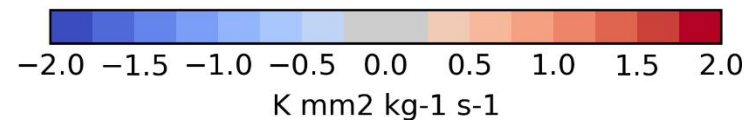
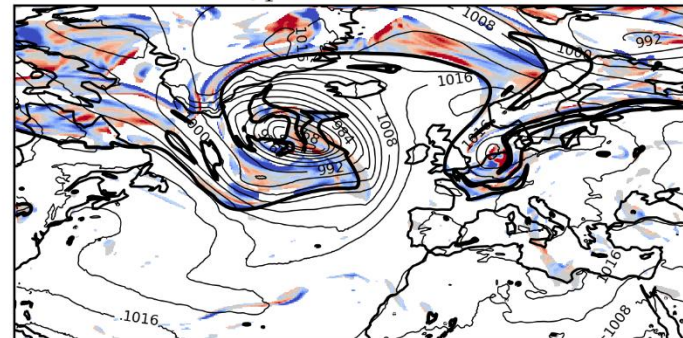
(b) $\Delta\theta_1^{s+1} > 8^{\text{th}}$ decile



(c) $\Delta Q_1^{s+1} < 2^{\text{nd}}$ decile



(d) $\Delta Q_1^{s+1} > 8^{\text{th}}$ decile



Lagrangian-tracer description

$$\langle \delta\varphi_{k+1}^s - \delta\varphi_1^{s+k} \rangle = - \langle \varphi_{0,k \rightarrow k+1}^s - \varphi_{0,0 \rightarrow 1}^{s+k} \rangle$$

Along-trajectory
modification

Advection

Upper levels (6.8 km – 11.2 km)

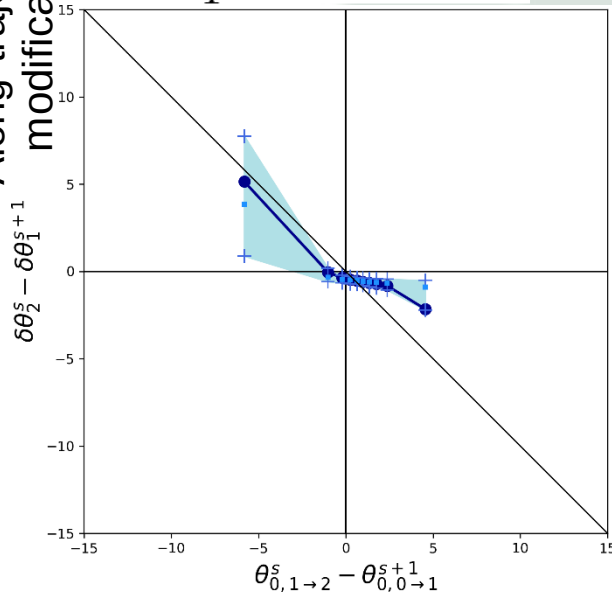
Potential temperature

Along-trajectory
modification

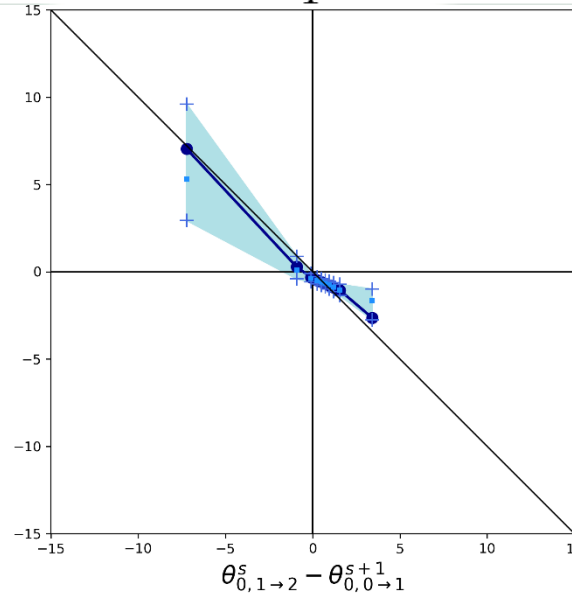
$\Delta\theta_1^{s+1} < 1^{\text{st}} \text{ decile}$

$4^{\text{th}} \text{ decile} < \Delta\theta_1^{s+1} < 6^{\text{th}} \text{ decile}$

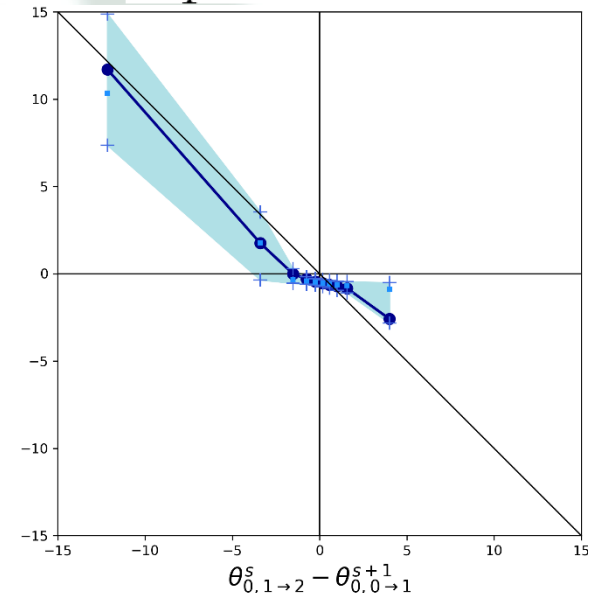
$\Delta\theta_1^{s+1} > 9^{\text{th}} \text{ decile}$



Advection



Advection



Advection

Lagrangian-tracer description

$$\langle \delta\varphi_{k+1}^s - \delta\varphi_1^{s+k} \rangle = - \langle \varphi_{0,k \rightarrow k+1}^s - \varphi_{0,0 \rightarrow 1}^{s+k} \rangle$$

Along-trajectory
modification

Advection

Upper levels (6.8 km – 11.2 km)

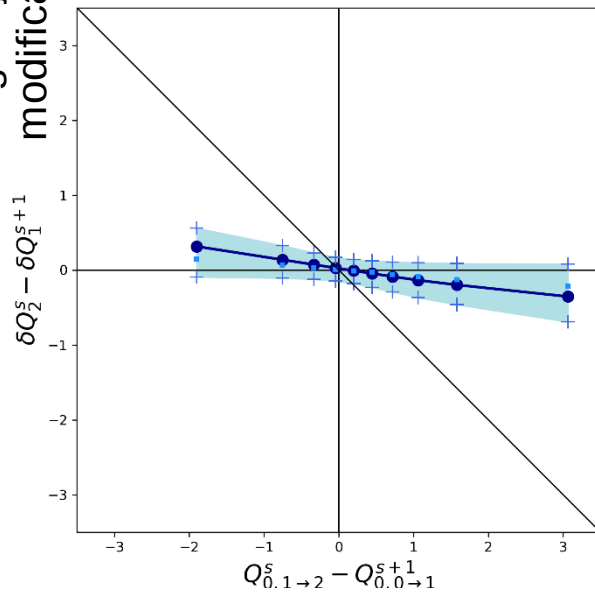
Potential vorticity

$\Delta Q_1^{s+1} < 1^{\text{st}} \text{ decile}$

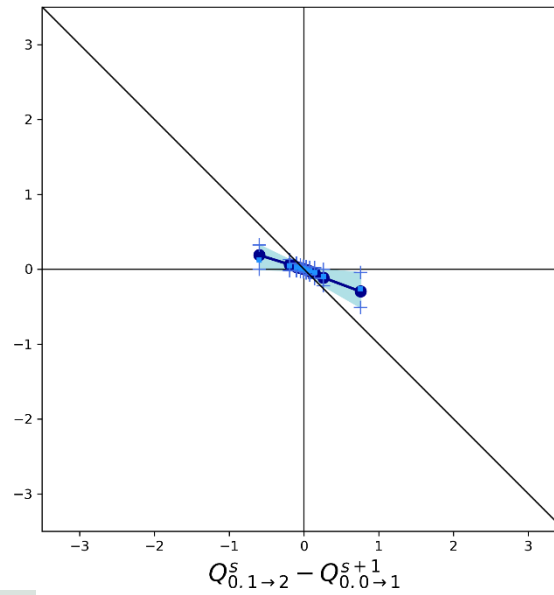
$4^{\text{th}} \text{ decile} < \Delta Q_1^{s+1} < 6^{\text{th}} \text{ decile}$

$\Delta Q_1^{s+1} > 9^{\text{th}} \text{ decile}$

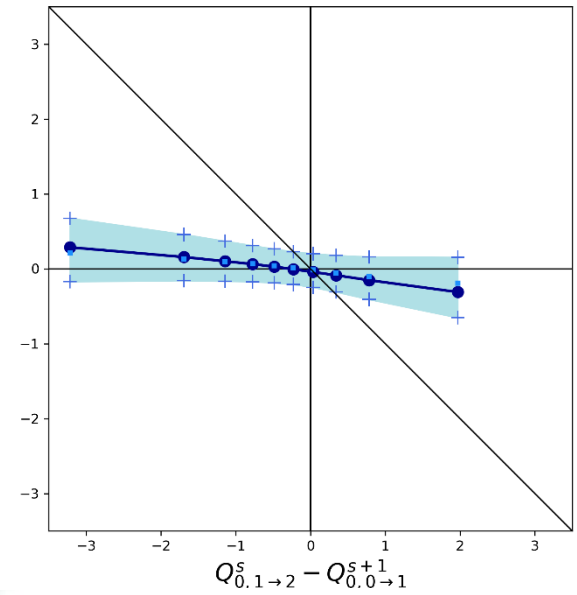
Along-trajectory
modification



Advection



Advection

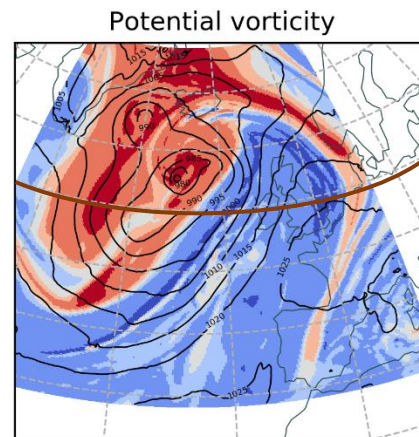
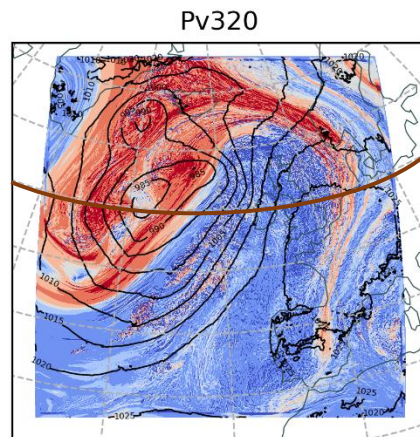


Advection

Conclusions

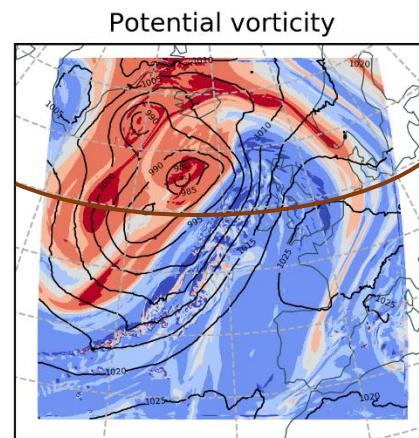
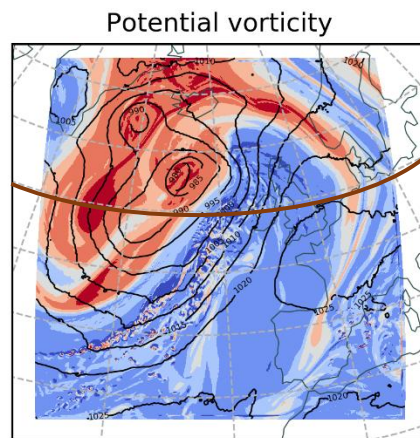
- Analysis of systematic errors in **changes** of potential temperature and PV using
 - An **Eulerian** description
 - A **Lagrangian-tracer** description
 - And a theoretical unbiased model's behaviour as a reference
- The largest **Eulerian** deviations in the long forecast correspond to the largest changes in the short forecast (i.e. **more dynamically active grid points**)
- Lagrangian tracers revealed that for PV, there was **a clear deviation** from the behaviour of the unbiased model regardless of the level of Eulerian change

T + 36
2-km
COSMO

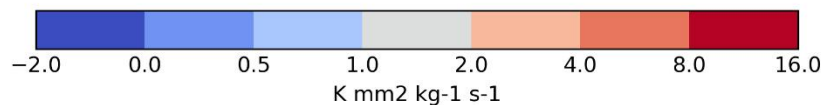


N768 UM
17-km

4.4-km UM
Smith



4.4-km UM
PC2

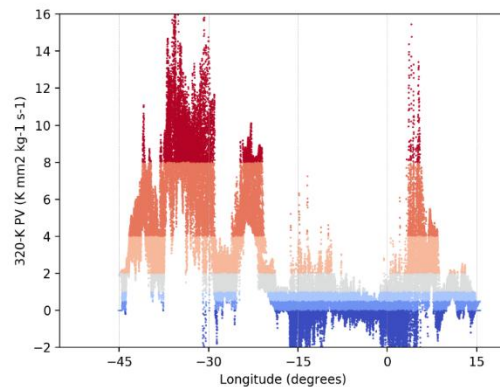


Collaborative work with Annika Oertel, Hanna Joos,
Claudio Sanchez and Ben Harvey

T + 36

2-km

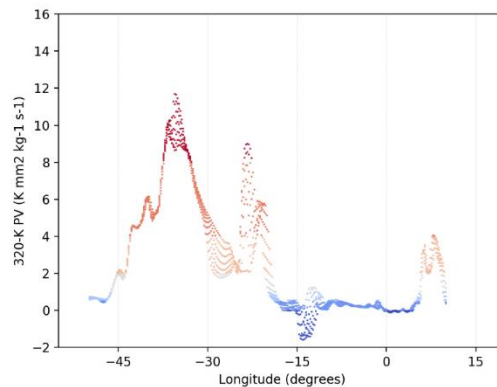
COSMO



1°-band centred on
54°N

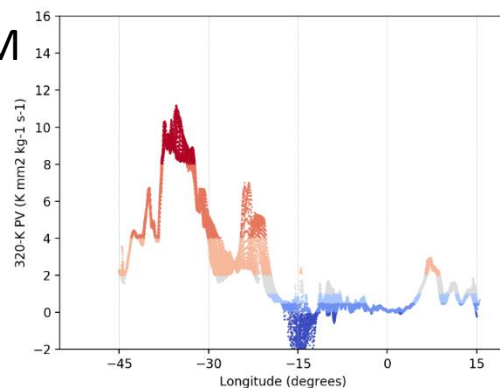
N768 UM

17-km



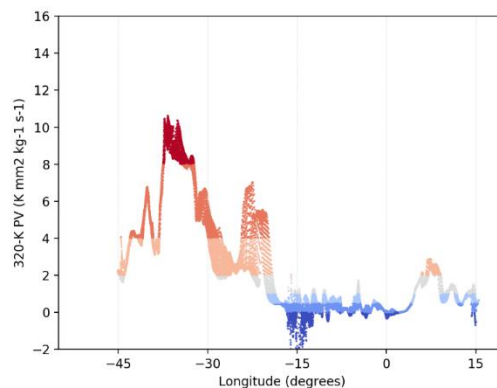
4.4-km UM

Smith



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